

Overview of Cellular CDMA

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Abstract—This paper is a general description of code division multiple access (CDMA). The analysis of power control schemes in CDMA is an original work. The wide-band wave propagation in the cellular environment presents an interesting result (the short-term fading reduction over the wide band-signal in cellular). Also less fading in urban areas than in suburban areas. The advantages of using CDMA listed in this paper have excited the cellular industry. Radio capacity is the key issue in selecting CDMA and is carefully described in this paper.

I. INTRODUCTION

THE development of the code division multiple access (CDMA) scheme is mainly for capacity reasons. Ever since the analog cellular system started to face its capacity limitation in 1987, the promotion of developing digital cellular systems for increasing capacity has been carried out. In digital systems, there are three basic multiple access schemes, frequency division multiple access (FDMA), time division multiple access (TDMA), and code division multiple access (CDMA). In theory, it does not matter whether the spectrum is divided into frequencies, time slots, or codes, the capacity provided from these three multiple access schemes is the same. However, in the cellular system, we might find that one may be better than the another. Especially in the North American Cellular System, no additional spectrum will be allocated for digital cellular. Therefore, the analog and digital systems will co-exist in the same spectrum. Also, the problem of transition from analog to digital is another consideration. Although the CDMA has been used in satellite communications, the same CDMA system cannot be directly applied to the mobile cellular system. In order to design a cellular CDMA system, we first need to understand the mobile radio environment; then study whether the characteristics of CDMA are suitable for the mobile radio environment or not; and finally describe the natural beauty of applying CDMA in cellular systems.

II. MOBILE RADIO ENVIRONMENT

The propagation of a narrow-band carrier signal is a conventional means of communication. However, in a CDMA system, the propagation of a wide-band carrier signal is used. Therefore, we first describe the propagation of the narrow-band wave, then of the wide-band wave.

A. Narrow-Band (NB) Wave Propagation

A signal transmitted from the cell-site and received by either a mobile unit or a portable unit would propagate over a

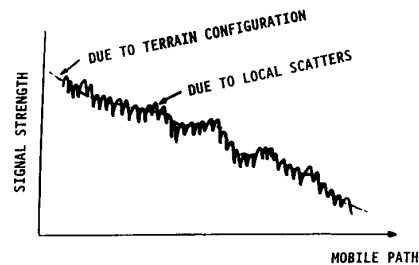


Fig. 1. Mobile radio environment.

particular terrain configuration between two ends. Therefore, the effect of the terrain configuration generates a different long-term fading characteristic which follows a log-normal variation appearing on the envelope of the received signal, as shown in Fig. 1. Since the antenna height of a mobile or portable unit is close to the ground, three effects are observed [1]. First, the signal received is not only from the direct path but also from the strong reflected path due to the fact that the antennas of the mobile units are close to the ground. These two paths create an excessive path loss which is 40 dB/dec (fourth power law applied), i.e., doubling the path loss in decibels of the free-space path loss. Second, under the low antenna height condition at the mobile units, the human-made structures surrounding them would generate the multipath fading on the received signal called Rayleigh fading, as shown in Fig. 1. The multipath fading causes the burst error in digital transmission. The average duration of fades \bar{t} as well as the level crossing rates \bar{n} at 10 dB below the average power of a signal is a function of vehicle speed V and wavelength λ .

$$\bar{t} = 0.132 \left(\frac{\lambda}{V} \right) \text{ s} \quad (1)$$

$$\bar{n} = 0.75 \left(\frac{V}{\lambda} \right) \text{ crossings/s.} \quad (2)$$

For a frequency of 850 MHz and a speed of 15 m/h then $\bar{t} = 6$ ms and $\bar{n} = 16$ crossings/s. Third, a time delay spread phenomenon exists due to the time dispersive medium. In a mobile radio environment a single symbol, transmitted from one end and received at the other end, receives not only its own symbol but also many echoes of its symbol. The time delay spread intervals are measured from the first symbol to the last detectable echo, which are different in human-made environments. The average time delay spread due to the local scatterers in suburban areas is 0.5 μ s and in urban areas is 3 μ s. These local scatterers are in the near-end region as illustrated in Fig. 2, and the time delay spread corresponding to this region is illustrated in Fig. 3. There are other types of

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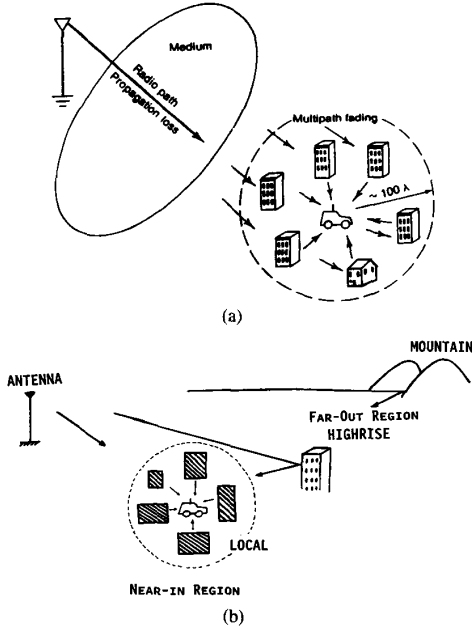


Fig. 2. (a) A mobile radio environment—two parts: propagation loss and multiple fading. (b) Time-delay spread scenario.

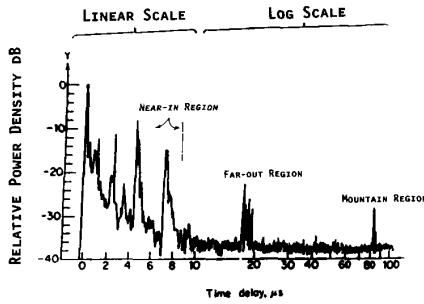


Fig. 3. An illustration on time-delay spread.

time delay spreads as illustrated in Fig. 2. One kind of delayed wave is due to the reflection of the high-rise buildings (far-out region), and one kind of delayed wave is due to the reflection from the mountains. Their corresponding time delays are illustrated in Fig. 3. In certain mountain areas, the time delay spread can be up to 100 μ s. These time delay spreads would cause intersymbol interference (ISI) for data transmission [2]. In order to avoid the ISI, the transmission rate R_b should not exceed the inverse value of the delay spread Δ if the mobile unit is at a standstill (nonfading case),

$$R_b < 1/\Delta \quad (3)$$

or R_b should not exceed the inverse value of $2\pi\Delta$ if the mobile unit is in motion (fading case)

$$R_b < 1/(2\pi\Delta). \quad (4)$$

If the transmission rate R_b is higher than (3) or (4), both FDMA and TDMA need equalizers which are capable of reducing the ISI to a certain degree depending on the hardness of the time delay spread length and the wave arrival

distribution [3]–[5]. An FDMA system always requires less transmission rate than a TDMA system if both systems offer the same radio capacity. Usually an FDMA system can get away from using an equalizer as long as its transmission rate does not exceed too much above 10 kilosamples per second. The CDMA system does not need an equalizer but a simpler device called a correlator will be used. It will be described later.

B. Wide-Band Wave Propagation [6]

1) *Path Loss*: Suppose that a transmitted power P_t in watts is used to send a wide-band signal with a bandwidth B in hertz along a mobile radio path r . The power spectrum over the bandwidth B is $S_t(f)$, then the P_t can be expressed as

$$P_t = G_t \int_{f_0 - \frac{B}{2}}^{f_0 + \frac{B}{2}} S_t(f) df. \quad (5)$$

The received power

$$P_r = \frac{P_t}{4\pi r^2} \times C(r, f) \times A_e(f) \quad (6)$$

where

$$C(r, f) = \text{medium characteristic} = k/(r^2 f) \quad (7)$$

$$A_e(f) = \text{effective aperture of the receiving antenna}$$

$$= \frac{c^2 G_r}{4\pi f^2} \quad (8)$$

k is a constant factor, c is the speed of light, G_t and G_r are the gains of the transmitting and receiving antennas, respectively. Substituting (5), (7), and (8) into (6), we obtain

$$P_r = \frac{kc^2 G_R G_t}{(4\pi r^2)^2} \int_{f_0 - \frac{B}{2}}^{f_0 + \frac{B}{2}} S_t(f) \frac{1}{f^3} df. \quad (9)$$

For simplicity but without losing much generality, let

$$S_t(f) = \text{constant}, \quad (10)$$

$$\text{for } f_0 - B/2 \leq f \leq f_0 + B/2.$$

Then (9) becomes

$$P_r = \frac{kc^2 G_t G_R}{(4\pi r^2)^2} \frac{1}{f_0^3 \left[1 - \left(\frac{B}{2f_0} \right)^2 \right]^2}. \quad (11)$$

Equation (11) is a general formula. For a narrow-band signal, $B \ll f_0$, then (11) becomes

$$P_r = \frac{kc^2 G_t G_R}{(4\pi r^2)^2 f_0^3} \quad (\text{narrow-band}). \quad (12)$$

From (11), we may find the B/f_0 ratio for the case of 1-dB difference in path loss between narrow-band and wide-band.

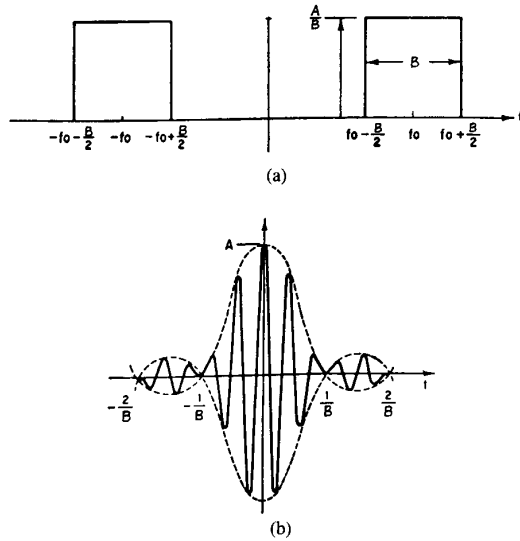


Fig. 4. Band-limited impulse. (a) Spectrum. (b) Waveshape.

That means by solving the denominator of (11) as follows:

$$10 \log \left[1 - \left(\frac{B}{2f_0} \right)^2 \right]^2 = -1 \text{ dB}$$

we obtain

$$B = 0.66 f_0.$$

In most wide-band applications, B will not be wider than $f_0/2$. Therefore, the narrow-band propagation path loss should be applied to the wide-band propagation path loss.

2) *Multipath Fading Characteristic on Wide-Band:* The wide-band pulse signaling $S_0(t)$ can be expressed as [7]

$$S_0(t) = A \frac{\sin(\pi B t)}{\pi t} \quad (13)$$

where A is the pulse amplitude shown in Fig. 4.

The received signal can be represented as

$$S(t) = (A/B) \sum_{m=-\infty}^{\infty} b_m(t) \frac{\sin \pi B \left(t - \frac{m}{B} \right)}{\pi \left(t - \frac{m}{B} \right)}. \quad (14)$$

The pulsewidth of $1/B$ is the time interval of the pulse occupied. Count all b_m that are not vanishing over a range of a finite number of m which is corresponding to a time delay spread Δ . Then the effective number of diversity branches, M , can be approximated by

$$M = \frac{\Delta + \frac{1}{B}}{\frac{1}{B}} = B \cdot \Delta + 1. \quad (15)$$

The effective number of diversity varies according to the human-made structures. The M is larger in the urban area than in the suburban area. Letting $\Delta = 0.5 \mu\text{s}$ for suburban and $\Delta = 3 \mu\text{s}$ for urban, and $B = 30 \text{ kHz}$ for narrow-band

and 1.25 MHz for wide-band, we find the effective number of diversity M in the following table.

Human-made environment	M diversity branches	
	$B = 30 \text{ kHz}$	$B = 1.25 \text{ MHz}$
$\Delta = 0.5 \mu\text{s}$	1.015	1.625
Suburban		
$\Delta = 3 \mu\text{s}$	1.09	4.75
Urban		

The wider the bandwidth, the less the fading. For $B = 1.25 \text{ MHz}$, the fading of its received signal is reduced as if the diversity-branch receiver which equals $M = 1.625$ (between a single branch and two branches) is applied in suburban areas, and $M = 4.75$ (between four and five branches) is applied in urban areas. The wide-band signal would provide more diversity gain in urban areas than in suburban areas. For $B = 30 \text{ kHz}$, no effective diversity gain is noticeable on its narrow-band received signal.

III. KEY ELEMENTS IN DESIGNING CELLULAR

The frequency reuse concept guides the cellular system design.

A. Cochannel Interference Reduction Factor (CIRF)

The minimum separation between two cochannel cells, D_s , is based on a cochannel interference reduction factor q which is expressed as

$$q = D_s/R \quad (16)$$

where R is the cell radius. The value of q is different for each system. For analog cellular systems, $q = 4.6$ is based on the channel bandwidth $B_c = 30 \text{ kHz}$ and the carrier-to-interference ratio (C/I) equals 18 dB.

B. Handoffs

The handoff is a unique feature in cellular. It switches the call to a new frequency channel in a new cell site without either interrupting the call or alerting the user. Reducing unnecessary handoffs and making necessary handoffs successfully are very important tasks for the cellular system operators in analog systems or in future FDMA or TDMA digital systems.

C. Frequency Management and Frequency Assignment

Based on the minimum distance D_s , the number of cells k , in a cell reuse pattern may be obtained,

$$K = (D_s/R)^2/3 = q^2/3. \quad (17)$$

The total allocated channels will be divided by K . There are K sets of frequencies; each cell operates its own set of frequencies managed by the system operator. This is the frequency management task. During a call process different frequencies are assigned to different calls. This is the frequency assignment task. Both tasks are critically impacted by interference and capacity.

D. Reverse-Link Power Control

The reverse-link power control is for reducing near-end to far-end interference. The interference occurs when a mobile unit close to the cell site can mask the received signal at the cell site so that the signal from a far-end mobile unit is unable to be received by the cell site at the same time. It is a unique type of interference occurring in the mobile radio environment.

E. Forward-Link Power Control

The forward-link power control is used to reduce the necessary interference outside its own cell boundary.

F. Capacity Enhancement

The capacity of cellular systems can be increased by handling q in two conditions.

- 1) Within standard cellular equipment—the value of q shown in (16) remains a constant. Reduce the cell radius R , thus D_s reduces. For a smaller D_s the same frequency can be used more often in the same geographical area: that is why we are trying to use small cells (sometimes called microcells or picocells) to increase capacity.
- 2) Chosen from different cellular systems—many different types of radio equipment can be chosen. Search for those cellular systems which can provide smaller values of q . When q shown in (16) is smaller, D_s can be less, even if the cell radius remains unchanged. We believe that q is smaller in properly designed digital cellular systems than q in analog systems. Choosing a smaller new q of a new system, we can increase the same amount of capacity without reducing the size of the cell based on the old q of an old system. That is why we are choosing a new digital system to replace the old analog system.

Reducing the size of cells in a system requires more cells. It is always costly. Therefore, the development of digital cellular systems properly is the right choice.

IV. SPREADING TECHNIQUES IN MODULATION

Spreading techniques in modulation are generally used in military systems for antijamming purposes. In general, there are two techniques: 1) spectrum spreading (spread spectrum) and 2) time spreading (time hopping) stated as follows:

A. Spread Spectrum (SS) Techniques

There are two general spread spectrum techniques, direct sequence (DS) and frequency hopping (FH).

1) *Direct Sequence*: In direct sequence, each information bit is symbolized by a large number of coded bits called chips. For example, if an information bit rate $R = 10$ kb/s is used and it needs an information bandwidth $B = 10$ kHz, and if each bit of 10 kb/s is coded by 100 chips, then the chip rate is 1 Mb/s which needs a DS bandwidth, $B_{ss} = 1$ MHz. The bandwidth is thus spreading from 10 kHz to 1 MHz. The spectrum spreading in DS is measured by the

processing gain (PG) in decibels

$$PG = 10 \log \frac{B_{ss}}{B} \quad (\text{in dB}). \quad (18a)$$

Then the PG of the above example is 20 dB. Or we say that this SS system has 20 dB processing gain. The first DS experiment was carried out in 1949 by DeRosa and Rogoff who established a link between New Jersey and California.

2) *Frequency Hopping*: An FH receiver would equip N frequency channels for an active call to hop over those N frequencies with a determined hopping pattern. If the information channel width is 10 kHz and there are 100 channels to hop, $N = 100$, the FH bandwidth $B_{ss} = 1$ MHz. The spectrum is spreading from 10 kHz (no hopping) to 1 MHz (frequency hopping). The spectrum spreading in FH is measured by the PG as

$$PG = 10 \log N \quad (\text{in dB}). \quad (18b)$$

Then the PG of the above example is 20 dB. The total hopping frequency channels are called chips. There are two basic hopping patterns; one called fast hopping which makes two or more hops for each symbol. The other called slow hopping which makes two or more symbols for each hop. In general, the transmission data rate is the symbol rate. The symbol rate is equal to the bit rate at a binary transmission. Due to the limitation of today's technology, the FH is using a slow hopping pattern.

B. Time Hopping

A message transmitted with a data rate of R requiring a transmit time interval T is now allocated at a longer transmission time interval T_s . In time T_s the data are sent in bursts dictated by a hopping pattern. The time interval between bursts t_n also can be varied. The time spreading data rate R_s is always less than the information bit rate R . Assume that N bursts occurred in time T , then

$$R_s = \left(\frac{T_s}{T} \right) R = \left(1 - \frac{\sum_1^N t_n}{T} \right) R. \quad (19)$$

V. DESCRIPTION OF DS MODULATION

The spread spectra (DS and FH) are used for reducing intentional interference (enemy jamming), and now we are using it for increasing capacity instead of reducing the intentional interference. Immediately we realize that the FH with a slow hopping does not serve the purpose of increasing capacity. The slow hopping is to let good channels downgrade and bad channels upgrade. In order to have a system design for capacity, all the channels have to be deployed only marginally well. If bad channels do occur in this high capacity SS system, the system does not provide normal channels with excessive signal levels which can average with the poor signal levels of those bad channels to within an acceptable quality level. It just pulls down all the channels to an unacceptable level. The proper way should be either drop the

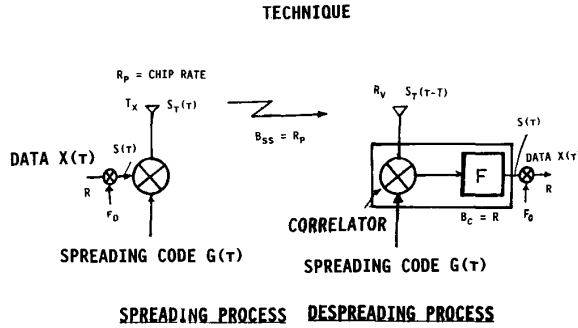


Fig. 5. Basic spread-spectrum technique.

bad channels or correct the bad channels by other means. The fast hopping does help increase the capacity because of its advantage of applying diversity but the technology to have fast hopping at 800 MHz is not available.

1) *Basic DS Technique:* The basic DS technique is illustrated in Fig. 5. The data $x(t)$ transmitted with a data rate R is modulated by a carrier f_0 first, then by a spreading code $G(t)$ to form a DS signal $S_i(t)$ with a chip rate R_p which takes a DS bandwidth $B_{SS} = R_p$. The DS signal $S_i(t - T)$ after a propagation delay T is received and goes through a correlator using the same spreading code $G(t)$ prestored in it to despread the DS signal. Then the despread signal $S(t - T)$ is obtained. After demodulating it by f_0 , $x(t)$ is recovered. Take a constant-envelope signal modulated on a carrier f_0 at transmitting end shown in Fig. 5. Let $x(t)$ be a data stream modulated by a binary phase shift keying (BPSK) that

$$x(t) = \pm 1 \quad (20)$$

modulated by a binary shift keying

$$S(t) = x(t) \cos(2\pi f_0 t). \quad (21)$$

At the transmitting end, the spreading sequence $G(t)$ modulation also uses BPSK

$$G(t) = \pm 1 \quad (22)$$

then

$$S_i(t) = x(t)G(t) \cos(2\pi f_0 t). \quad (23)$$

At the receiving end, the $S_i(t - T)$ is received after T seconds propagation delay. The despreading processing then takes place. The signal $S(t - T)$ coming out from the correlator is

$$S(t - T) = x(t - T) \cdot G(t - T)G(t - \hat{T}) \cos(2\pi f_0(t - T)) \quad (24)$$

where \hat{T} is the estimated propagation delay generated in the receiver. Since $G(t) = \pm 1$,

$$G(t - T)G(t - \hat{T}) = 1 \quad (25)$$

from a good correlator $T = \hat{T}$. Then

$$S(t - T) = x(t - T) \cos(2\pi f_0(t - T)). \quad (26)$$

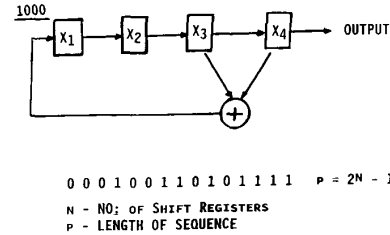


Fig. 6. PN code (linear maximal length sequence) generator.

After it is demodulated by the carrier frequency f_0 , the data $x(t - T)$ then are recovered as shown in Fig. 5.

2) *Pseudonoise (PN) Code Generator:* Pseudonoise code coming from a PN sequence is a deterministic signal [8]. For example, the sequence 000100110101111 is a PN sequence. It contains three properties.

- a) *Balance property:* 7 zeros and 8 ones. The numbers of zeros and ones of a PN code are different only by one.
- b) *Run property:* There are four “zero” runs (or “one” runs): runs = 4.
 1/2 of runs (i.e., 2) of length 1; i.e., two single “zeros (or ones).”
 1/4 of runs (i.e., 1) of length 2; i.e., one “2 consecutive zeros (or ones).”
 1/8 of runs (i.e., 0.5) of length 3; i.e., one “3 consecutive zeros (or ones).” In the above example, 1/8 of runs cannot be counted for too short a code.
- c) *Correlation property:* Let D denote the “difference,” and S denote the “same” by comparing two PN codes as follows:

$$\begin{array}{r} 000100110101111 \\ 100010011010111 \\ \hline DSSDDSDSDDDDSSS \end{array}$$

The value of the correlation of two N -bit sequences can be obtained by counting the number N_d of D 's and the number N_s of S 's and inserting them into the following equation:

$$P = \frac{1}{N}(N_s - N_d) = \frac{1}{15}(7 - 8) = -\frac{1}{15}. \quad (27)$$

Then the correlation of a 15-b PN code is $-1/15$. The PN code generator of a four-shift register is shown in Fig. 6. The modulo 2 adder is summing the shift register X_3 and the shift register X_4 . The summing signal then feeds back to the shift register X_1 . Suppose that a 4-b sequence 1000 is fed into the shift register X_1 . The output PN sequence from this PN code generator is 00010011010111. The code length L of any PN code generator is dependent upon the number of shift registers N :

$$L = 2^N - 1. \quad (28)$$

The PN sequence generated in Fig. 6 is also called the linear maximal length sequence. For $N = 4$, L is 15.

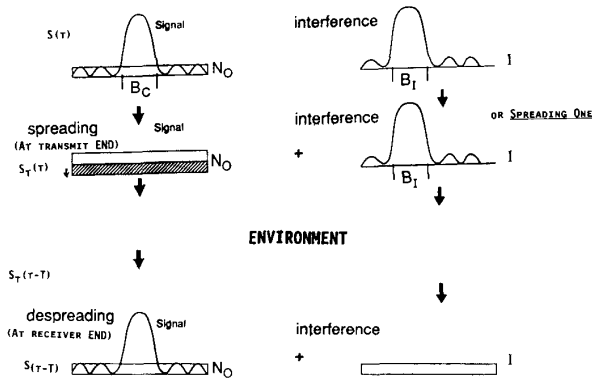


Fig. 7. Spread spectrum.

3) *Reduction of Interference by a DS signal:* The signal $S(t)$ of Fig. 5, before the spreading processing can be illustrated in both the frequency and time domains, is shown in Fig. 7. After spreading $S(t)$ with a given $G(t)$, the output $S_r(t)$ is transmitted out while the interference in the air could be a narrow-band signal or a DS signal with a different $G_r(t)$. When $S_r(t - T)$ is received after a propagation delay T , it is despreading with the same $G(t)$ and obtaining $S(t - T)$. The interference signal would spread to an SS signal by the $G(t)$ if it was a narrow-band signal, or stay as an SS signal because $G(t)$ and $G_r(t)$ do not agree with each other. Thus as a result, a low level of interference within the desired signal bandwidth B_c can be achieved.

VI. MULTIPLE ACCESS SCHEMES

The multiple access schemes are used to provide resources for establishing calls. There are five multiple access schemes. *FDMA* serves the calls with different frequency channels. *TDMA* serves the calls with different time slots. *CDMA* serves the calls with different code sequences. *PDMA* (polarization division multiple access) serves the calls with different polarization. *PDMA* is not applied to mobile radio [6]. *SDMA* (space division multiple access) serves the calls by spot beam antennas. The calls in different areas covered by the spot beams can be served by the same frequency—a frequency reuse concept. In the cellular system, the first three multiple access schemes can be applied. The illustration of the differences among three multiple access schemes are shown in Fig. 8. Assume that a set of six channels is assigned to a cell. In *FDMA*, six frequency channels serve six calls. In *TDMA*, the channel bandwidth is three times wider than that of *FDMA* channel bandwidth. Thus two *TDMA* channel bandwidths equal six *FDMA* channel bandwidths. Each *TDMA* channel provides three time slots. The total of six time slots serve six calls. In *CDMA*, one big channel has a bandwidth equal to six *FDMA* channels. The *CDMA* radio channel can provide six code sequences and serve six calls. Also, *CDMA* can squeeze additional code sequences in the same radio channel, but the other two multiple access schemes cannot. Adding additional code sequences, of course, degrades the voice quality.

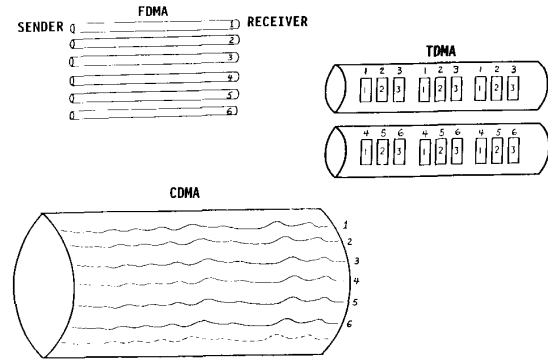


Fig. 8. Illustration of different multiple access systems.

A. Carrier-to-Interference Ratio (C/I)

In analog systems, only *FDMA* can be applied. The C/I received at the RF is closely related to the S/N at the baseband which is related to the voice quality. In digital systems, all three, *FDMA*, *TDMA*, and *CDMA* can be applied. The C/I received at the RF is closely related to the E_b/I_0 at the baseband.

$$\begin{aligned} C/I &= (E_b/I_0)(R_b/B_c) \\ &= (E_b/I_0)/(B_c/R_b) \end{aligned} \quad (29)$$

where E_b is the energy per bit; I_0 is the interference power per hertz, R_b is the bit per second, and B_c is the radio channel bandwidth in hertz. In digital *FDMA* or *TDMA* there are designated channels or time slots for calls. Thus R_b equals B_c and E_b/I_0 at the baseband is always greater than one, then C/I is also greater than one, i.e., a positive value in decibels. In *CDMA*, all the coded sequences say N , share one radio channel; thus B_c is much greater than R_b . The notation B_c is often replaced by B_{ss} which is the spread-spectrum channel. Within the radio channel, any one code sequence is interfered with $N-1$ of other code sequences. Therefore, the interference level is always higher than the signal level. C/I is less than one, i.e., a negative value in decibels.

B. Capacity of Cellular *FDMA* and *TDMA* [9]

In *FDMA* or *TDMA*, each frequency channel or each time slot is assigned to one call. During the call period, no other calls can share the same channel or slot. In this case, the cochannel interference would come from a distance of $D_s = qR$. Assume that the worst case of having six cochannel interferers (see Fig. 9) and the fourth power law pathloss are applied. The capacity of the cellular *FDMA* and cellular *TDMA* can be found by the radio capacity m expressed as

$$m = \frac{B_t/B_c}{K} = \frac{M}{\sqrt{\frac{2}{3} \left(\frac{C}{I} \right)_s}} \text{ number of channels/cell} \quad (30)$$

where

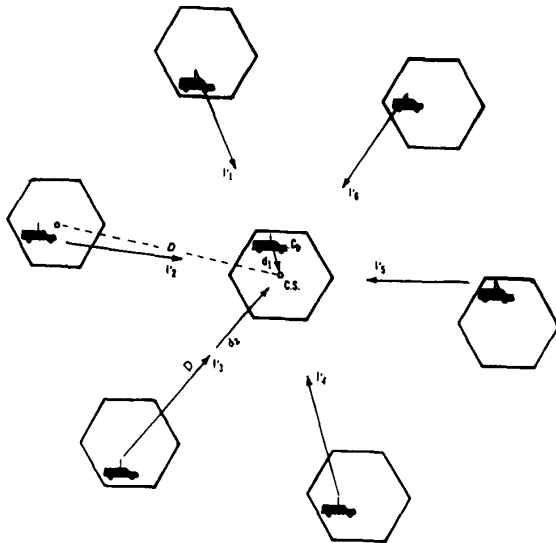


Fig. 9. Cochannel interference.

- B_t total bandwidth (transmitted or received),
- B_c channel bandwidth (transmitted or received) or equivalent channel bandwidth,
- $M = B_t/B_c$ total number of channels or equivalent channels,
- $(C/I)_s$ minimum required carrier-to-interference ratio per channel or per time slot.

Equation (30) can be directly applied to both analog FDMA and digital FDMA systems. In TDMA systems, B_c is an equivalent channel bandwidth. For example, a TDMA radio channel bandwidth of 30 kHz with three time slots can have an equivalent channel bandwidth of 10 kHz ($B_c = 10$ kHz). Therefore the minimum required $(C/I)_s$ of each time slot turns out to be the same as $(C/I)_s$ of the TDMA equivalent channel. The radio capacity is based on two parameters, B_c and $(C/I)_s$ as shown in (30). It has the same two parameters as appear in Shannon's channel capacity formula. The difference between (30) and Shannon's is that the two parameters are related in the former one and independent in the latter one. The $(C/I)_s$ of radio capacity can be found based on a standard voice quality as soon as the channel bandwidth B_c is given.

C. Radio Capacity of Cellular CDMA

Cellular CDMA is uniquely designed to work in cellular systems. The primary purpose of using this CDMA is for high capacity. In cellular CDMA, there are two CIRF values. One CIRF is called adjacent CIRF, $q_a = D_s/R = 2$. It means that the same radio channel can be reused in all neighboring cells. The other CIRF is called self-CIRF, $q_s = 1$. It means that different code sequences use the same radio channel to carry different traffic channels. The two CIRF's are shown in Fig. 10. With the smallest value of CIRF, the CDMA system is proven to be the most efficient frequency-reuse system we can find.

1) *Required $(C/I)_s$ in Cellular CDMA:* $(C/I)_s$ can be found from (29) depending on the value of E_b/I_0 which is

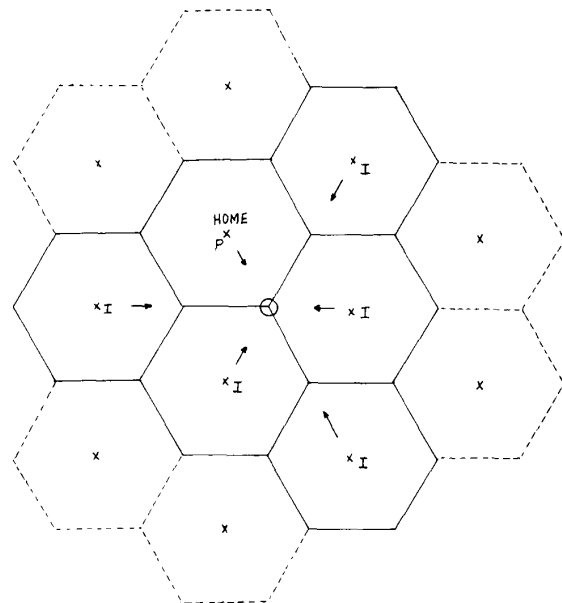


Fig. 10. CDMA system and its interference.

measured at the baseband determined by the voice quality. For example, the vocoder rate is $R_b = 8$ kb/s and the total wide-band channel bandwidth $B_t = 1.25$ MHz, then if E_b/I_0 is determined as follows:

$$E_b/I_0 = 7 \text{ dB, then } (C/I)_s = 0.032$$

$$E_b/I_0 = 4.5 \text{ dB, then } (C/I)_s = 0.01792.$$

The radio capacity of this system can be derived as follows. It can be calculated based on the forward link, and can also be further improved by the power control schemes.

2) *Without Power Control Scheme:* The radio capacity is calculated from the forward link C/I ratio. The $(C/I)_s$ received by a mobile unit at the boundary of a CDMA cell shown in Fig. 10 can be obtained based on nine interfering cells as follows:

$$\begin{aligned}
 (C/I)_s &= \frac{\alpha \cdot R^{-4}}{\underbrace{\alpha(M-1) \cdot R^{-4}}_{\text{within the cell}} + \underbrace{\alpha \cdot 2M \cdot R^{-4}}_{\text{two closest adjacent cells}} \\
 &\quad + \underbrace{\alpha \cdot 3M \cdot (2R)^{-4}}_{\text{three intermediate-range cells}} + \underbrace{\alpha \cdot 6M(2.633R)^{-4}}_{\text{six distant cells}} \\
 &= \frac{1}{3.3123M - 1} \tag{31}
 \end{aligned}$$

where α is a constant factor, M is the number of traffic channels. $(C/I)_s$ can be determined based on E_b/I_0 and R_b/B_s as shown in (29). Then M can be found from (31)

$$(C/I)_s = 0.032 \quad M = 9.736$$

$$(C/I)_s = 0.01792 \quad M = 17.15.$$

The radio capacity defined in (30)

$$m = \frac{M}{K} \text{ number of traffic channels/cell.} \quad (32)$$

In this case $K = q_a^2/3 = 4/3 = 1.33$. Therefore,
 $m = M/1.33 = 7.32$ traffic channels/cell for $E_b/I_0 = 7$ dB
 $= 12.9$ traffic channels/cell for $E_b/I_0 = 4.5$ dB.

3) *With Power Control Scheme*: We can increase the radio capacity by using a proper power control scheme. The power control scheme used at the forward link of each cell can reduce the interference to the other adjacent cells. The less the interference generated in a cell, the more the value of M increases. In (31), we notice that if we can neglect all the interference, then, as shown in Fig. 10

$$(C/I)_s = \frac{R^{-4}}{(M-1)R^{-4}} = \frac{1}{M-1} \quad (33)$$

for

$$(C/I)_s = 0.032 \quad M = 30.25$$

$$(C/I)_s = 0.01792 \quad M = 54.8.$$

Comparing (31) with (33), the total number of traffic channels M is drastically reduced due to the existence of interference. However, since interference is always existing in the adjacent cells, we can only reduce it by using a power control scheme. By using a power control scheme the total power after combining all traffic channels should be considered in two cases. a) The necessary power delivery to the close-in mobile unit and b) The total power reduced at the boundary.

- a) The necessary power delivery to a close-in mobile unit. The transmitted power at the cell site for the j th mobile unit is P_j , which is proportional to r_j^n .

$$P_j \propto r_j^n \quad (34)$$

where r_j is the distance between the cell site and the j th mobile unit. n is a number. In examining the number n , we find that the power control scheme of using $n = 2$ in (34) can provide the optimum capacity and also meet the requirement that the forward link signal can still reach the near-end mobile unit at distance r_j from the cell site with a reduced power

$$P_j = P_R \left(\frac{r_j}{R} \right)^2 \quad (35)$$

where P_R is the power required to reach those mobile units at the cell boundary R . The M mobile units served by M traffic channels are assumed uniformly distributed in a cell. Then

$$p(M_i) = kr_i, \quad 0 \leq r_i \leq R \quad (36)$$

where $M = \sum_{l=1}^L M_l$. There are L groups of mobile units. Each one of L is equally circled around the cell site. Where M_l is the number of mobile units in the l th group depending on its location. k is a constant. Equation (36) indicates that fewer mobile units are closely circling around the cell site, more mobile units are at the outside ring of the cell site. Assume that the distance r_0 is from the cell site to a desired mobile unit, also assume that r_0 is a near-in distance between the mobile unit and the cell site. With the help of (34) and (35) the power transmitted from the cell site, P_t , is equal to

$$\begin{aligned} P_t &= \sum_{M_1} P_1 + \sum_{M_2} P_2 + \sum_{M_3} P_3 + \cdots + \sum_{M_L} P_L \\ &= P_R \left[\sum_{kr_1} \left(\frac{r_1}{R} \right)^2 + \sum_{kr_2} \left(\frac{r_2}{R} \right)^2 + \cdots + \sum_{kr_L} \left(\frac{r_L}{R} \right)^2 \right] \\ &= P_R \left[kr_1 \left(\frac{r_1}{R} \right)^2 + kr_2 \left(\frac{r_2}{R} \right)^2 + \cdots + kr_L \left(\frac{r_L}{R} \right)^2 \right]. \end{aligned} \quad (37)$$

Since r_L is the distance from the cell site to the cell boundary, $r_L = R$ then (37) becomes

$$P_t = P_R k \int_0^R \frac{r^3}{R^2} dr = P_R k \frac{R^2}{4}. \quad (38)$$

The total number of mobile units M can be obtained as

$$\begin{aligned} M &= \sum_{i=1}^L M_i = k(r_1 + r_2 + \cdots + R) \\ &= k \int_0^R r dr = k \frac{R^2}{2}. \end{aligned} \quad (39)$$

Substituting (39) into (38):

$$P_t = P_R k \left[\frac{M}{2k} \right] = P_R \frac{M}{2}. \quad (40)$$

If the full power P_R is applied to every channel, then

$$P_t = MP_R. \quad (41)$$

Comparing (40) and (41), the total transmitted power reduces to one-half by using the power control scheme of (35). The $(C/I)_s$ of a mobile unit at a distance of r_0 which is close to the cell site is

$$(C/I)_{s1} = \frac{P_R (r_0/R)^2 \cdot r_0^{-4}}{P_R (M/2) \cdot r_0^{-4}} = \frac{(r_0/R)^2}{(M/2)}. \quad (42)$$

The interference from the adjacent cells can be neglected in (42) in this case.

- b) The total power is reduced at the cell boundary. The $(C/I)_s$ of a mobile unit at a distance R which is at the cell boundary can be obtained similarly to (31).

$$(C/I)_{s2} = \frac{P_R}{P_R \left[\frac{M-1}{2} + 2 \frac{M}{2} + 3 \left(\frac{M}{2} \right) \cdot (2)^{-4} + 6 \left(\frac{M}{2} \right) (2.633)^{-4} \right]} = \frac{1}{1.656M}. \quad (43)$$

The values of M and m can be found from (43) for the case of applying the power control scheme.

$$\begin{aligned} M &= 18.87, m = 14.19, (C/I) = 0.032 \text{ (-15 dB)} \\ M &= 23.7, m = 28.33, (C/I) = 0.01792 \text{ (-17 dB)}. \end{aligned} \quad (44)$$

At this time, $(C/I)_s$ received by the mobile unit at the distance r_0 from (42) should be checked with (43) to see whether it is valid or not.

$$(C/I)_{s1} = \frac{(r_0/R)^2}{M/2} = \frac{3.3(r_0/R)^2}{3.3(M/2)} \geq \frac{1}{1.656M}. \quad (45)$$

In (44), the power reduction ratio $(r/R)^2$ has to be not less than 0.302 for those mobile units located less than the distance r_0 which is 0.55R. If we set the lowest power to be 0.302 P_R then the total power has to be changed.

$$\begin{aligned} P_t &= P_R k \left[\frac{r_0^2}{R^2} r_1 + \frac{r_2^3}{R^2} + \frac{r_3^3}{R^2} + \dots \right] \\ &= P_R k \left[\left(\frac{r_0}{R} \right)^2 \int_0^{r_0} r dr + \int_{r_0}^R \frac{r^3}{R^2} dr \right] \\ &= P_R k \frac{R^2}{4} \left[1 + \left(\frac{r_0}{R} \right)^4 \right]. \end{aligned} \quad (46)$$

For $r_0/R = 0.55$, then $(r_0/R)^4 = 0.0913$.

The transmitted power P_t in (46) has to be adjusted as

$$P_t = P_R k (R^2/4) \times 1.0913 = P_R (M/2) \times 1.0913. \quad (47)$$

Equation (47) indicates that by setting the condition of the lowest power per traffic channel to be 0.302 P_R at the cell site to serve the mobile units within and equal to the distance r_0 , $r_0 = 0.55R$, the total power at the cell site is slightly increased by 1.0913 times as compared with (38). Under the adjusted transmitted power P_t as shown in (47), the actual values of M and m are reduced.

$$\begin{aligned} M &= 18.87/1.0913 = 17.3, \\ m &= 13 \quad \text{for } (C/I)_s = 0.032 \\ M &= 33.7/1.0913 = 30.9, \\ m &= 25.96 \quad \text{for } (C/I)_s = 0.1792. \end{aligned} \quad (48)$$

Comparing (48) with (44), we find no significant change of M and m when the adjusted transmitted power is applied.

D. Comparison of Different Cases in CDMA

Table I lists the performance of five different cases:

- Case 1:* No adjacent cell interference is considered (this is not a real case).
- Case 2:* No power control, adjacent cell interference is considered.
- Case 3:* Power control with $n = 1$, adjacent cell interference is considered.

Case 4: Power control with $n = 2$, adjacent cell interference is considered.

Case 5: Power control with $n = 3$, adjacent cell interference is considered.

In Table I, Case 1 is not a real case. In Case 2, without power control, the performance is poor. The power control schemes are used in Cases 3–5. In these cases, in order to provide the minimum transmitted power at the cell site for serving those mobile units within or equal to the distance of r_0 , the total transmitted power at the cell site increases as indicated under the heading “after adjusting the transmitted power.” Comparing the number of channels per cell m among Cases 3–5, we found that Case 4 has two channels more than Case 3 but one channel less than Case 5. However, Case 5 is harder to implement than Case 4. One channel gained in Case 5 over Case 4 can be washed out in the practical situation. When the power control schemes of $n > 3$ are used, no further improvement in radio capacity is found. Therefore, we conclude that $n = 2$ in Case 4 is a better choice.

VII. REDUCTION OF NEAR-FAR RATIO INTERFERENCE IN CDMA

In CDMA, all traffic channels are sharing one radio channel. Therefore a strong signal received from a near-in mobile unit will mask the weak signal from a far-end mobile unit at the cell site. To reduce this near-far ratio interference, a power control scheme should be applied on the reverse link. As a result, the signals received at the cell site from all the mobile units within a cell remain at the same level. The scheme is described as follows. The power transmitted from each mobile unit has to be adjusted based on its distance from the cell site, as

$$P_j = P_R \left(\frac{r_j}{R} \right)^4 \quad (49)$$

where P_R , r , and R are mentioned previously, and a fourth power rule is applied in (49). Neglecting the interfering signals from adjacent cell, the C/I received from a mobile unit J , at the cell site can be obtained as

$$C/I = \frac{P_R \left(\frac{r_j}{R} \right)^4 (r_j)^{-4}}{\sum_1^{M-1} P_R \left(\frac{r_j}{R} \right)^4 (r_j)^{-4}} = \frac{1}{M-1}. \quad (50)$$

The C/I of (48) has to be greater than or equal to the required $(C/I)_s$,

$$C/I \geq (C/I)_s. \quad (51)$$

Applying (51) in (50), we obtain

$$\begin{aligned} M &= 30.25, m = 22.74, \quad \text{for } (C/I)_s = 0.032 \text{ (-15 dB)} \\ M &= 54.5, m = 41.2, \quad \text{for } (C/I)_s = 0.01792 \text{ (-17 dB)}. \end{aligned}$$

The number of channels M obtained from the reverse link is much higher than that from the forward channel as shown in Table I. It indicates that the effort is to increase the number of channels on the forward link for more radio capacity.

TABLE I

Performance in Different Cases	Adjacent Cell Interfering				No Adjacent Cell Interference is Considered Case 1	
	No Power Control	Power Control Schemes				
	Case 2 $N = 0$	Case 3 $N = 1$	Case 4 $N = 2$	Case 5 $N = 3$		
Power Control due to the distance from the cell site	P_R	$P_R(r_j/R)$	$P_R(r_j/R)^2$	$P_R(r_j/R)^3$	P_R	
R_0	N/A	$0.303R$	$0.55R$	$0.7R$	N/A	
Before adjusting the TX power	Total Transmitted Power at the Cell Site	MP_R	$P_R(2M/3)$	$P_R(M/2)$	$P_R(2M/5)$	MP_R
	The $(C/I)_s$ Received at R_0	$\frac{1}{M-1}$	$(r_0/R)/(2M/3)$	$(r_0/R)^2/(M/2)$	$(r_0/R)^3/(2M/5)$	$\frac{1}{M-1}$
	At R (Cell Boundary)	1	1	1	1	1
		$3.3123M - 1$	$2.2M$	$1.656M$	$1.32M$	$M - 1$
	M at $(C/I)_s = 0.032$	9.736	14.2	18.87	23.67	30.25
	$(C/I)_s = 0.0179$	17.15	25.36	33.7	42.27	54.8
	M at $(C/I)_s = 0.032$	7.32	10.67	14.19	17.8	22.74
	$(C/I)_s = 0.0179$	12.9	19	28.33	31.78	41.2
	Total Transmitted Power at the Cell Site		$P_R(2M/3) \times 1.0139$	$P_R(M/2) \times 1.09$	$P_R(2M/5) \times 1.25$	
	The $(C/I)_s$ Received		$(r_0/R)/[(2M/3) \times 1.0139]$	$(r_0/R)^2/[(M/2) \times 1.09]$	$(r_0/R)^3/[2M/5 \times 1.25]$	
at $R \leq R_0$		$(r/R)/[(2M/3) \times 1.0139]$	$(r/R)^2/[(M/2) \times 1.09]$	$(r/R)^3/[2M/5 \times 1.25]$		
at $R > R_0$		1	1	1		
at R		$2.23M$	$1.8M$	$1.65M$		
M at $(C/I)_s = 0.032$ (-15 dB)		14.2	17.3	19		
at $(C/I)_s = 0.010792$ (-17.4 dB)		25.36	31	33.8		
m at $(C/I)_s = -15$ dB		10.67	13	14		
at $(C/I)_s = -17.4$ dB		19	23.3	25.4		

VIII. NATURAL ATTRIBUTES OF CDMA [10]

There are many attributes of CDMA which are of great benefit to the cellular system.

- 1) Voice activity cycles: The real advantage of CDMA is the nature of human conversation. The human voice activity cycle is 35%. The rest of the time we are listening. In CDMA all the users are sharing one radio channel. When users assigned to the channel are not talking, all others on the channel benefit with less interference in a single CDMA radio channel. Thus the voice activity cycle reduces mutual interference by 65%, increasing the true channel capacity by three times. CDMA is the only technology that takes advantage of this phenomenon. Therefore, the radio capacity shown in (48) can be three times higher due to the voice activity cycle. It means that the radio capacity is about 40 channels per cell for $C/I = -15$ dB or $E_b/I_0 = 7$ dB.
- 2) No equalizer needed: When the transmission rate is much higher than 10 kb/s in both FDMA and TDMA, an equalizer is needed for reducing the intersymbol interference caused by time delay spread. However, in CDMA, only a correlator is needed instead of an equalizer at the receiver to despread the SS signal. The correlator is simpler than the equalizer.
- 3) One radio per site: Only one radio is needed at each site or at each sector. It saves equipment space and is easy to install.
- 4) No hard handoff: Since every cell uses the same CDMA radio, the only difference is the code sequences. Therefore, no handoff from one frequency to another frequency while moving from one cell to another cell. It is called a soft handoff.
- 5) No guard time in CDMA: The guard time is required in TDMA between time slots. The guard time does occupy the time period for certain bits. Those waste bits could be used to improve quality performance in TDMA. In CDMA, the guard time does not exist.
- 6) Sectorization for capacity: In FDMA and TDMA, the utilization of sectorization in each cell is for reducing the interference. The trunking efficiency of dividing channels in each sector also decreases. In CDMA, the sectorization is used to increase capacity by introducing three radios in three sectors and therefore, three times the capacity is obtained as compared with one radio in a cell in theory.
- 7) Less fading: Less fading is observed in the wide-band

signal while propagating in a mobile radio environment. More advantage of using a wide-band signal in urban areas than in suburban areas for fading reduction as described in Section II-B.

- 8) Easy transition: In a situation where two systems, analog and CDMA, have to share the same allocated spectrum, 10% of the bandwidth (1.25 MHz) will increase two times ($= 0.1 \times 20$) of the full bandwidth of FM radio capacity as shown below. Since only 5% (heavy users) of the total users take more than 30% of the total traffic, the system providers can let the heavy users exchange their analog units for the dual mode (analog/CDMA) units and convert 30% of capacity to CDMA on the first day of CDMA operations.
- 9) Capacity advantage: Given that

$$B_t = 1.25 \text{ MHz, the total bandwidth}$$

$$B_{ss} = 1.25 \text{ MHz the CDMA radio channel}$$

$$B_c = 30 \text{ kHz for FM}$$

$$B_c = 30 \text{ kHz and three time slots for TDMA.}$$

Capacity of FM $1.25/30 = 41.6$

$$\text{total numbers of channels} = \frac{1.25 \times 10^6}{30 \times 10^3}$$

$$= 41.67 \text{ channels}$$

$$\text{the cell reuse pattern } K = 7$$

$$\text{the radio capacity } m_{\text{FM}} = \frac{41.67}{7} = 6$$

channels/cell.

Capacity of TDMA

$$\text{total number of channels} = \frac{1.25 \times 10^6}{10 \times 10^3} = 125$$

channels

$$\text{the cell reuse pattern } K = 4 \text{ (assumed)}$$

$$\text{the radio capacity } m_{\text{TDMA}} = \frac{125}{4} = 31.25$$

channels/cell.

Capacity of CDMA

$$\text{total number of channels / cell, } m = 13$$

$$\text{the cell reuse pattern } K = 1.33$$

$$\text{the radio capacity, take (48) at } E_b/I = 7 \text{ dB}$$

add voice activity cycle and sectorization,

$$m_{\text{CDMA}} = 13 \times 3 \times 3 \approx 120 \text{ channels/cell.}$$

Therefore,

$$m_{\text{CDMA}} = 20 \times m_{\text{FM}}$$

$$= 4 \times m_{\text{TDMA}}$$

- 10) No frequency management or assignment needed: In FDMA and TDMA, the frequency management is always a critical task to carry out. Since there is only one common radio channel in CDMA, no frequency management is needed. Also, the dynamic frequency would implement in TDMA and FDMA to reduce real-time interference, but needs a linear broad-band power amplifier which is hard to develop. CDMA does not need the dynamic frequency assignment.
- 11) Soft capacity: In CDMA, all the traffic channels share one CDMA radio channel. Therefore, we can add one

additional user so the voice quality is just slightly degraded as compared to that of the normal 40-channel cell. The difference in decibels is only $10 \log \frac{41}{40}$ which is 0.24 dB down in C/I ratio.

- 12) Coexistence: Both systems, analog and CDMA can operate in two different spectras, and CDMA only needs 10 % of bandwidth to general 200 % of capacity. No interference would be considered between two systems.
- 13) For microcell and in-building systems: CDMA is a natural waveform suitable for microcell and in-building because of being susceptible to the noise and the interference.

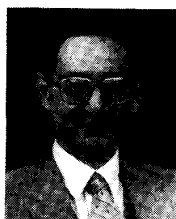
IX. CONCLUSION

The overview of CDMA highlights the potential of increasing capacity in future cellular communications. This paper describes the mobile radio environment and its impact on narrow-band and wide-band propagation. The advantage of having CDMA in cellular systems is depicted. The concept of radio capacity in cellular is also introduced. The power control schemes in CDMA have been carefully analyzed. The natural attributes of CDMA provide the reader with the reasons that cellular is considering using it. This paper leads the reader to understand two CDMA papers [11], [12], which are analyzed in more depth in this issue, and to build interest in CDMA by reading other references [13]–[19].

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